

3.12

$$\vec{E} = \hat{x}xy - \hat{y}(x^2 + 2y^2)$$

$$a) \oint \vec{E} \cdot d\vec{l}$$

$$= \int_{x=0}^1 xy dx - \int_0^1 (x^2 + 2y^2) dy + [\int xy dx - \int (x^2 + 2y^2) dy]$$
$$= -1$$

$$b) \nabla \times \vec{E} = \begin{vmatrix} \hat{x} & \hat{y} & \hat{z} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ xy & -(x^2 + 2y^2) & 0 \end{vmatrix} = -3x\hat{z}$$

$$\int \nabla \times \vec{E} \cdot d\vec{s} = \int_{x=0}^1 \int_{y=0}^x -3x dx dy = -1$$